



Term(s)	Definition	Example	Most common use?
algebra tiles	Algebra tiles allow students to better understand ways of algebraic thinking and the concepts of algebra. They are a concrete representation of how algebra works. https://www.youtube.com/watch?v=8 mZMssxt54A	(x - 2)	6 th : Understand that positive and negative numbers are used together to describe quantities having opposite directions or values, write expressions that record operations with numbers and letters standing for numbers, apply properties of operations to generate equivalent espressions, identify when two expressions are equivalent
area model	An area model is a model for math problems where the length and width of an array are used as factors to find the product, or total area, of the array. https://www.youtube.com/watch?v=5 QZnVBlMhNs	10 + 3 10 • 10 10 • 10 10 • 3 20 = 2 • 10 30 = 10 • 3 100 = 10 • 10 156	3 rd : Represent multiplication with an area model 4 th : Illustrate multiplication with area models 5 th : Illustrate division with an area model, illustrate subtraction of decimals, illustrate multiplication with an area model.
array	An array is an ordered arrangement of a product (total) shown in rows and columns. https://www.youtube.com/watch?v=c7UwNboK0I8	6 X 18 = 108	3 rd : Represent multiplication with an area model 4 th : Illustrate multiplication with area models 5 th : Illustrate division with an area model, illustrate additiona nd subtraction of decimals, illustrate multiplication with an area model.
attribute blocks	Attribute blocks are used to practice sorting. A set of attribute blocks includes triangles, circles, squares, and rectangles of differing sizes and colors. https://www.youtube.com/watch?v= L-qWSXCUdbg		 K: Name shapes, analyze and compare shapes, compose simple shapes to form larger shapes. 1st: Compose shapes to create a composite shape. 2nd: Recognize shapes that have specified attributes.

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base ten materials: units, strips, mats, dimension pieces	Base ten blocks are used by students to learn patterning, addition, subtraction, number sense, place value, multiplication, area, and division. Units are the square pieces representing the ones place. Strips are ten units put together, representing the tens place. Mats are ten strips put together, representing the 100s place. Dimension pieces are little black segments used to define an array. https://www.youtube.com/watch?v=u jEGPx_BlNU https://www.youtube.com/watch?v= Y7qkyMyanjU		K: Make numbers from 11-19 1 st : Represent two-digit numbers as tens and ones, add within 100, subtract multiples of 10 2 nd : Add and subtract within 100, represent numbers as hundreds, tens,and ones. Add and subtract within 1000 3 rd : Represent multiplication with an area model 4 th : Illustrate multiplication with area models 5 th : Illustrate division with an area model, illustrate additiona nd subtraction of decimals, illustrate multiplication with an area model
bundle (group)	In our math system, units are bundled or grouped into tens, hundreds, thousands, etc. Mathematicians designed bundling units, tens, etc. as an efficient way of counting. https://www.youtube.com/watch?v=-MU3idwwLBY		K: Make numbers from 11-19 1st: Represent two-digit numbers as tens and ones, add within 100, subtract multiples of 10 2nd: Add and subtract within 100, represent numbers as hundreds, tens, and ones. Add and subtract within 1000
compose	To compose means to build, or put together, to create a whole. Numbers and shapes are examples of math concepts that can be composed. https://www.youtube.com/watch?v=DFBM8NKuftU https://www.youtube.com/watch?v=QqTqlMsYeI	12+12+12=36 6 triangles can be grouped to form a hexagon 4 groups of 9 = 36 2 parallelograms can form a hexagon	All grade levels

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cubes	One-inch and one-centimeter cubes are commonly used to teach volume of prisms (three-dimensional shapes made from shapes such as triangles, squares, etc). Students are able to create a prism shape and then use the cubes to fill the shape. By counting the number of cubes used, students can determine the volume of the shape. https://www.youtube.com/watch?v=ubucii-7yg8		5 th : Measure volume by counting unit cubes (cubic cm and cubic inches) 6 th : Find the volume of right rectangular prisms
decimal	A decimal is an equal part of a whole number based on denominators that are limited to powers of 10. Decimals are written as numbers after a decimal point. https://www.youtube.com/watch?v=J4w2spaCky4	$ \begin{array}{cccc} 0.5 & 0.72 & 0.638 \\ \downarrow \uparrow & \downarrow \uparrow & \downarrow \uparrow \\ \hline \frac{5}{10} & \frac{72}{100} & \frac{638}{1000} \end{array} $	4 th : Use decimal notation for fractions with denominators 10 or 100, compare two decimals to hundredths by reasoning about their size 5 th : Read, write, and compare decimals to the thousandths; add, subtract, and divide decimals to the hundredths 6 th : Fluently add, subtract, multiply, and divide multi-digit decimals
decompose	To decompose a number means to break it down into component parts. There are multiple ways to decompose numbers. Shapes can also be decomposed . https://www.youtube.com/watch?v=k Rt0zjTut-Q https://www.youtube.com/watch?v=k VQqL01GBSxE	Decompose 36 12+ 12+12	All grade levels
efficiency	Efficiency in math means selecting tools and procedures in order to perform mathematics in the best possible manner with the least amount of time or effort. https://www.youtube.com/watch?v=2 ZKiJXvAuI8	Students who are efficient in using arithmetic strategies will not count on their fingers to find the answer to 8+9. They will use an addition strategy such as make a ten (9+1 +10, then add 7 more).	All grade levels

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equivalent fractions	Equivalent fractions name the same value, even though they have different numerators and denominators. https://www.youtube.com/watch?v=g EzbI82B9QI	$\frac{2}{3}$ $\frac{4}{6}$	 3rd: Explain equivalence of fractions 4th: Explain why fractions are equivalent 5th: Use equivalent fractions as a strategy to add and subtract fractions 6th: Apply and extend previous understandings of equivalent fractions
factor	A factor is a number that is multiplied by another number to make a product. https://www.youtube.com/watch?v=9 ZENZShozik	$5 \times 4 = 20$ 5 and 4 are both factors of 20	 3rd: Fluently multiply and divide within 100 4th: Find all factor pairs for a whole number in the range 1-100 6th: Find the greatest common factor of two whole numbers less than or equal to 100
five frame	A five frame is a table consisting of 5 cells. Young children learn basic addition and subtraction using the 5 frame as a concrete tool and reference. https://www.youtube.com/watch?v=J w8hgAPrACM		K: Fluently add and subtract within 5
fraction	A fraction is a numerical quantity that is less than one whole. The denominator defines how many equal pieces make a whole. The numerator explains how many equal pieces of the whole are being used, named, or defined by the fraction in question. https://www.youtube.com/watch?v=4 67 s6nDBfA https://www.youtube.com/watch?v=Ix72WMHYWas https://www.youtube.com/watch?v=SxmkVsJxnMk	1 1/2 1/4 3/4	1st: Partition circles and rectangles into two and four equal shares 2nd: Partition circles and rectangles into two, three, or four equal shares 3rd: Understand fractions and unit fractions, understand equivalent fractions, compare fractions with same numerators or denominators 4th: Explain fraction equivalencies, compare fractions with different numerators and denominators decompose fractions into unit fractions 5th: Add and subtract fractions with unlike denominators, solve word problems involving addition, subtraction of fractions 6th: Interpret and compute quotients of fractions, and solve word problems involving the division of fractions by fractions

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fraction bars and fraction circles	Sets of fraction bars or fraction circles provide visual illustration of math operations using fractions of whole numbers. They are also useful in understanding equivalent fractions. https://www.youtube.com/watch?v=- ve_CN511UM https://www.youtube.com/watch?v=y SGOJSR06fc	1/2 1/2 1/2 1/3 1/3 1/3 1/3 1/4 1/4 1/4 1/4 1/5 1/5 1/5 1/5 1/5 1/5 1/6 1/6 1/6 1/6 1/6 1/6 1/6 1/8 1/8 1/8 1/8 1/8 1/8 1/8 1/8 1/0 1/0 1/0 1/0 1/0 1/0 1/0 1/0 1/0 1/0	3 rd : Understand fractions and unit fractions, understand equivalent fractions, compare fractions with same numerators or denominators 4 th : Explain fraction equivalencies, compare fractions with different numerators and denominators decompose fractions into unit fractions 5 th : Add and subtract fractions with unlike denominators, solve word problems involving addition and subtraction of fractions 6 th : Interpret and compute quotients of fractions, and solve word problems involving the division of fractions by fractions
geoblocks	Geoblocks are three-dimensional shapes used to teach students about geometrical features such as corners, edges, faces, symmetry, area, congruence, etc. https://www.youtube.com/watch?v=i_8zqc-hKMM		K: Name shapes, analyze and compare shapes 1 st : compose shapes to create a composite shape 2 nd : Recognize shapes that have specified attributes
graduated cylinders, beakers	Graduated cylinders or beakers are standard measuring tools used to develop understanding of liquid volume. https://www.youtube.com/watch?v=f WWLOzrjjJw		3 rd : Measure liquid volumes using standard units of liters, solve one-stepword problems involving volumes given the same units 4 th : know relative sizes of units (liter and milliliter), solve word problems involving masses 5 th : convert among different-sized standard measurement units: mL to liters, liters to mL

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Judy Clocks	A specific brand of clock, the Judy Clock has an hour hand that moves according to the minute hand. This mimics the movement of traditional classroom clocks and is used to help students understand the functions of the hour and minute hands. https://www.youtube.com/watch?v= Oa3vybzZa6s	10 12 1 9 3 8 7 5	1 st : Tell time to the hour and half-hour 2 nd : Tell time to the nearest five minutes 3 rd : Tell time to the nearest minute
linking cubes	Linking cubes are multicolored, two-centimeter cubes that can be attached together to make towers. https://www.youtube.com/watch?v=a T 3ew-4Yfc		K: Count and compare the number of objects, represent addition and subtraction with objects, use objects to show decomposition of numbers, find numbers that will make ten 1 st : Represent addition and subtraction, connect to find the length of an object 2 nd : Determine whether a group of objects is odd or even
math journal	A math journal is a place for students to write down their mathematical reasoning. Math journals can be notebooks, binders, folders, etc. https://www.youtube.com/watch?v=z zEiwsO7rtw	The short of violation and the first of the short of the	All grade levels
multiple	A multiple is a number that can be divided by another number without any remainder. https://www.youtube.com/watch?v= ZO9PnNyAfcY	$5 \times 4 = 20$ 20 is a multiple of 5 and 4	4 th : Determine whether a given whole number in the range 1-100 is a multiple of a given one-digit number 6 th : Find the least common multiple of two whole numbers less than or equal to 12

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money	Money refers to standard US currency and coins: pennies, nickels, dimes, quarters, half-dollars, and dollars. https://www.youtube.com/watch?v=9 https://www.youtube.com/watch?v=9 https://www.youtube.com/watch?v=9	THE STATE OF THE S	2 nd : Solve word problems involving money *After second grade, word problems include situations involving money, but money is not mentioned as a standard
number bonds	A number bond is a simple addition sum that can be recognized and completed almost instantly. Another term for number bonds is fact family. <a href="https://www.youtube.com/watch?v=" https:="" td="" watch?v="https://www.youtube.com/watch?v=" www.yo<="" www.youtube.com=""><td>3, 5, and 8 form a number bond: 3+5=8 5+3=8 Which can also be extended to subtraction: 8-5=3 8-3=5</td><td>K: Fluently add and subtract within 5 1st: Fluently add and subtract within 10 2nd: Fluently add and subtract within 20</td>	3, 5, and 8 form a number bond: 3+5=8 5+3=8 Which can also be extended to subtraction: 8-5=3 8-3=5	K: Fluently add and subtract within 5 1 st : Fluently add and subtract within 10 2 nd : Fluently add and subtract within 20
number talks	Number talks are a teaching strategy designed to help students use their math reasoning to add, subtract, multiply and divide mentally. https://www.youtube.com/watch?v= RCPo334nPbQ https://www.youtube.com/watch?v= DQtgFaVqv7c	How would you solve 9x16 mentally? Lia used friendly numbers: 9x16 11 (group of 16) 10x16=160 160-16=144 Michael fractors: 9x16 9x16 9x16 9x16 9x16 9x16 9x16 9x18 12x2 12x2=144	All grade levels
open number line	An open number line is a visual representation for recording and sharing students' thinking strategies during the process of mental computation. It can be created at any point along the continuum of numbers. https://www.youtube.com/watch?v=ucDucqYbffs	$\frac{25 + (31)}{41} = ?$	Begins in 2 nd grade with the introduction of the ruler as a measuring tool. This is students' first exposure to numbers ordered sequentially in a line. From this first use of the ruler, students begin using the number line as a tool to explain mental math calculations.

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pattern blocks	Pattern blocks are color-coded geometric shapes—yellow hexagons, tan and blue parallelograms, red trapezoids, orange squares, and green triangles. Pattern blocks are frequently used in geometry and fraction lessons. https://www.youtube.com/watch?v=p J938Z4QrTY		K: Name shapes, analyze and compare shapes, compose simple shapes to form larger shapes 1 st : Put shapes together to create a new form 2 nd : Recognize shapes that have specified attributes (corners, angles, sides, etc.)
percent	Percent means how many parts out of one hundred. Percents can be converted to fraction and decimal representations. https://www.youtube.com/watch?v=1 CNZE8E48TA	Fraction Decimal Percent	6 th : Find a percent of a quantity as a rate per 100
protractor	A protractor is a standard measuring tool used to measure the angle created when two lines intersect, or meet. <a href="https://www.youtube.com/watch?v=t] 4xCOUNEInI</td><td>150 10 10 10 10 10 10 10 10 10 10 10 10 10</td><td>4<sup>th</sup>: Measure angles in whole-number degrees using a protractor</td></tr><tr><td>rate</td><td>A rate is a special ratio in comparing two different units. The word per can replace the equal sign. https://www.youtube.com/watch?v=c 6NQrt01dQQ	1 minute = 60 seconds 1 hour = 60 minutes (or) 3600 seconds 1 day = 24 hours (or) 1440 minutes	6 th : Understand the concept of a unit rate associated with a ratio, use rate language in the context of a ratio relationship, use ratio and rate reasoning to solve real-world and mathematical problems

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ratio	A ratio is a relationship between two numbers of the same kind. Ratios are usually expressed in the form <i>a:b</i> .	John's pocket money to Mark's pocket money	John: Mark II:9	6th: Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantitites, use
	They can also be expressed as fractions of a total. https://www.youtube.com/watch?v=	Mark's pocket money to John's pocket money	Mark: John 9:11	ratio and rate reasoning to solve real-world and mathematical problems
	TR5_eqmcp6c	John's pocket money as a fraction of the total pocket money	John 11 20	
		Mark's pocket money as a fraction of the total pocket money	$\frac{\text{Mark}}{\text{total}}$ $\frac{9}{20}$	
rebundle (regroup)	Rebundling or regrouping occurs during computation, especially addition, subtraction, and multi-digit multiplication. It involves composing a new bundle and moving it over to the next place value or decomposing a bundle and moving it back into a preceding place value. https://www.youtube.com/watch?v= TEyeYm2wxz0	Tens On-		2 nd : Use place value understanding and properties of operations to add and subtract 3 rd , 4 th : Use place value understanding and properties of operations to perform multi-digit arithmetic 5 th : Perform operations with multi-digit whole numbers and with decimals to hundredths 6 th : Compute fluently with multi-digit numbers
ruler	A ruler is a standard measuring tool. Rulers can be straight edged but a tape measure is also a type of ruler. Rulers typically measure in inches and centimeters. Longer rulers, called yardsticks or meter sticks, measure in inches, centimeters, feet, and meters. https://www.youtube.com/watch?v=f OtOWPHcHUg	THE THE PARTY OF T	N N N N N N N N N N N N N N N N N N N	2 nd : Measure length of objects using standard measuring tools 3 rd : Measure to the half and fourth of an inch 4 th : Know relative sizes of units: meter and cm, foot, inch and yard; measure to the nearest half, fourth, and eighth inch 5 th : Convert among different-sized units: inch to feet, cm to meter, foot to yard, Measure to the nearest half, fourth, and eighth

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spring scale	A spring scale is a standard measuring tool used to determine the mass of objects. https://www.youtube.com/watch?v=twelb8y5vrg	76543	3 rd : Measure masses of objects using standard units of grams and kilograms, solve one-step word problems involving masses of the same units 4 th : Know relative sizes of units (grams, kilograms, pounds, ounces), Solve word problems involving masses 5 th : Conver among different sized standard measurement units (grams/kilograms)
square inch tiles	Square inch tiles are usually multi- colored and made from acrylic or plastic. https://www.youtube.com/watch?v =BdBI27EpjhI		K: Count and compare objects 1 st : Show addition and subtraction with objects, lay tiles end to end to show length of an object 2 nd : Determine if a group is odd or even, arrange tiles in arrays 3 rd : Represent multiplication as equal groups, represent division as making equal groups, represent multiplication as an array, measure area by counting unit squares
student models	Student models are how students show their mathematical reasoning about a problem. Models can include using manipulatives, sketches, diagrams, etc. https://www.youtube.com/watch?v=jzq-kuyhiqs	Number Line Model 3x 5=15 (Three hops of five land on fifteen.)	All grades
subitize	Subitize means to instantly recognize the quantity in a group of objects without having to count them. Most people are able to recognize the quantity in a group of up to 5 objects instantaneously. https://www.youtube.com/watch?v=9 CsiwqujK-8		K: Compare numbers; count to tell the number of objects

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ten frame	A ten frame is two five frames put	Ten Frame	K: Understand addition as putting together
	together. This is a tool used to build		and adding to, and understand subtraction
	number sense and basic addition and		as taking apart and taking from; work with
	subtraction fluency.		numbers 11-19 to gain foundations for
	https://www.youtube.com/watch?v=p		place value
	<u>6RaMGDPfJg</u>		1 st : Add and subtract within 20;
			understand place value
two-colored	Two-colored counters are circles		K: Count and compare the number of
counters	with a different color on each side.		objects, represent addition and subtraction
	These counters can be used to		with objects, use objects to decompose
	compose and decompose numbers		numbers, find the number that will make
	and represent addition and		ten
	subtraction.		1 st : Represent addition and subtraction
	https://www.youtube.com/watch?v=_		with objects
	D6bk0GvvXA		2 nd : Determine whether a group of objects
			is odd or even